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HAS GREATER STOCK MARKET PARTICIPATION INCREASED WEALTH INEQUALITY IN THE US?

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Is wider access to stockholding opportunities related to reduced wealth inequality, given that it creates challenges for small and less sophisticated investors? Counterfactual analysis is used to study the influence of changes in the U.S. stockholder pool and economic environment, on the distribution of stock and net household wealth during a period of dramatic increase in stock market participation. We uncover substantial shifts in stockholder pool composition, favoring smaller holdings during the 1990s upswing but larger holdings around the burst of the Internet bubble. We find no evidence that widening access to stocks was associated with reduced net wealth inequality.

JEL Codes: E21, G11

Keywords: financial literacy, household finance, stockholding, wealth inequality

1. Introduction

Household investments in risky assets, especially direct and indirect stock holdings, grew substantially between the late 1980s and 2001 in the U.S.¹ By early 2000s about half of households had invested in stocks, partly in response to stockholding opportunities introduced through individual retirement accounts

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¹For participation trends in the U.S. since the 1980s, see Bertaut and Starr-McCluer (2002). Christelis, Georgarakos and Haliassos (2013) examine such links for 13 different countries, while they study patterns for the different stockholding modes available in the U.S. in Christelis, Georgarakos and Haliassos (2011).

and defined contribution pension plans but also to reduced costs of investing in mutual funds.²

A sizeable expansion of the stockholder base, such as the one recorded in the U.S. throughout the 1990s, is often thought of as facilitating wealth enhancement and reduction in wealth inequality by widening access to the equity premium. However, stocks are complicated and management-intensive financial instruments. As a result, they tend to create challenges, especially for households entering the stock market with limited resources, experience, information, and financial sophistication. Indeed, if enough unsophisticated investors enter and jeopardize their limited savings previously held in safe accounts, then increased access might result in a more unequal distribution of wealth.

Existing literature has established that certain household characteristics (e.g. higher wealth and education) increase the likelihood of stock market participation.³ A largely unexplored implication of this is that, when stockholding participation spreads, the composition of the stockholder pool in terms of investors' characteristics and of their respective tendencies to allocate wealth to stocks can also change. A natural candidate episode for studying such changes and their repercussions on wealth inequality is the period 1989–2001 in the U.S., that witnessed a continuous expansion of the stockholder pool in the face of dramatic stock price increases followed by the burst of the Internet bubble.

In this paper, we use three waves of the U.S. Survey of Consumer Finances (SCF) between 1989 and 2001 that record an increase in stock market participation and distinguish between the stock market upswing (1989, 1998) and the aftermath of the downswing (2001).⁴ The paper has three novel features. First, we employ econometric methods of counterfactual analysis to decompose changes in the entire distribution of stockholding levels into changes in a) the composition of the U.S. stockholder pool, in terms of characteristics, attitudes, and practices, over these periods, and b) the contribution of these characteristics to stockholding levels. We show that changes in the composition of the US stockholder pool have played a key role in shaping the distribution of equity wealth holdings. In particular, we find evidence that during the stock market upswing between 1989 and 1998, there was a shift in the composition of the stockholder pool towards characteristics systematically related to smaller stockholding levels. Yet, stock market entries and exits around the burst of the Internet bubble resulted, by 2001, in a stockholder pool with owner characteristics typically related to more sizeable stock holdings.

²The role of defined contribution pension plans, especially 401(k) plans, as a vehicle for spreading stock market participation during the boom is stressed in an Investment Company Institute and Securities Industry Association report entitled "Equity Ownership in America, 2005". Duca (2005) documents a rise in equity participation rates through mutual funds (outside of pension accounts) that can be linked to reduced costs of investing in mutual funds. Such decline in mutual fund costs is also likely to lower the relative costs of offering a defined contribution pension plan, thus contributing to the rise in (indirect) stock market participation via the pension channel.

³See, for example, Haliassos and Bertaut (1995), Cocco, Gomes and Maenhout (2005), Heaton and Lucas (2000), Gollier (2001), Campbell and Viceira (2002), Haliassos and Michaelides (2003), and Gomes and Michaelides (2005). Behavioral finance perspectives to the issue of stockholding are reviewed by Barberis and Thaler (2003).

⁴According to the SCF, stock market participation peaked in 2001 (51.9 percent) relative to only 31.8 percent in 1989. Stockholding rates in subsequent waves were relatively stable or somewhat declined: 48.6 percent in 2004, 51.2 percent in 2007, and 49.8 percent in 2010.

The second novel feature of the paper is that we estimate that a significant part of these relevant changes in the composition of the stockholder pool refer to changes in investors' financial attitudes and practices likely to be linked to financial literacy and sophistication.

Third, we examine the contribution of stockholding levels to changes in net wealth inequality over this important period. We show that inequality in stock holdings became quantitatively important for overall net wealth inequality, despite the relatively small share of stocks in household wealth. We find this to be in contrast with the limited importance of the typically largest component of wealth, namely primary residence. Notwithstanding the importance of stocks, we do not find evidence that widening access to the stock market during this period, notably through the spread of defined contribution plans, individual retirement accounts and mutual funds, was associated with a progressively less unequal distribution of either stock wealth or net wealth.

Our findings have implications for different strands of recent literature. Theoretical literature on stock market participation and wealth inequality is rather limited, but already points to conflicting effects. Some papers emphasize that broadening access to an instrument offering an expected return premium would tend to reduce wealth inequality, while others point to ambiguities in the distributional effect arising from endogenous information acquisition (Arrow, 1987; Peress, 2004; Guvenen, 2006).6 Favilukis (2013) points to a conflict between increasing participation (which tends to lower wealth inequality by making the equity premium available to more investors) and stock market boom (which tends to widen the wealth gap between stockholders and non-stockholders). The period we examine was characterized by large changes both in participation and in stock returns. Our empirical investigation suggests that the movement in stock returns dominated the expansion of the stockholder base in determining the overall outcome for wealth inequality. This is consistent with our findings on the changing composition of the stockholder pool, namely that smaller investors were drawn into the pool at the time of the stock market upswing, as these are less likely to experience large wealth gains from the equity premium. It is also consistent with the significant changes in stock wealth inequality that we find among owners of stocks.7

In addition to considerations relevant for the size of stock holdings, there is cumulating evidence of differential financial sophistication and tendency of certain

⁵Wealth inequality is of interest both in its own right and because households at different points of the wealth distribution tend to exhibit different financial behavior. Hurst and Lusardi (2004) have documented that a positive relationship between wealth and entry into entrepreneurship can be found only at the top five percentiles of the wealth distribution. Carroll (2001) showed that richer households are not simply blown-up versions of poorer households. Wolff (1998) shows that only the top 20 percent of households enjoys higher mean net worth and financial wealth levels between 1983 and 1995, while the other groups undergo real wealth or income losses with the shortfall being more severe for the poor.

⁶Guvenen shows that limited stock market participation can account for much of U.S. wealth inequality, which suggests that expanding participation should reduce wealth inequality. Ambiguities arise, however, even in stylized models once full financial information and sophistication are not taken for granted among all participating households (Peress, 2004). For effects of stock market participation regarding market volatility and stock market trading, see Pagano (1989), Allen and Gale (1994), Herrera (2001). For effects on the equity premium, see for example Heaton and Lucas (1999).

⁷See table 4 below.

demographic groups to mishandle stock investments. Such tendencies could further limit the wealth gains from entering the stock market. Campbell (2006) argues that households with lower education and resources are more prone to "investment mistakes" in terms of (non)participation, (under)diversification, and (lack of) debt refinancing. Poor understanding of finances has been shown to be more prevalent among females, minorities, and low-education households with limited finances and has been linked to lack of planning for retirement in data covering the older subset of the U.S. population (Lusardi and Mitchell, 2007). The study of van Rooij, Lusardi, and Alessie (2011) links stockholding participation directly to indicators of financial literacy. Feeling less financially competent has been shown more prevalent among females and those with lower education and has been linked to lack of international diversification in a study of U.S. investors with at least \$10,000 in total investments (Graham, Harvey, and Huang, 2009).

Calvet, Campbell, and Sodini (2007) study a unique administrative data set on the population of Swedish households. They find that, although the median Sharpe ratio attained by Swedish participants is close to that attainable by a global equity index, there is significant cross-sectional variation, with low education and low-wealth households likely to exhibit lower Sharpe ratios. Van Rooij, Lusardi and Alessie (2012), using Dutch survey data, show that higher financial literacy is associated with higher levels of wealth in a given year. They attribute this to the role of financial literacy in facilitating access to stocks (i.e. an asset with wealth gaining potential) and thus to more efficient retirement planning.

The rest of the paper is organized as follows. Section 2 provides information on the data used and applies counterfactual decomposition techniques to investigate whether the spread of equity culture drew progressively smaller stockholders into the stockholder pool. Section 3 measures the contribution of various asset components to net total wealth inequality and its evolution over a period of growing participation that encompasses the stock market upswing followed by a downswing. Section 4 offers concluding remarks.

2. Increased Participation and the Transformation of the Stockholder Pool

Given the nature of our research questions, we use data from the SCF that span the entire population and not only a subset (such as older households interviewed in the Health and Retirement Study, or owners of sizeable investment accounts recorded in administrative data sources). The SCF exhibits two features that are key to our analysis: it oversamples the rich, who own the largest share of wealth; and it is not subject to top coding of wealthy households. As a result, the SCF covers almost the full range of the wealth distribution and can describe well the wealthy households who hold the bulk of stock wealth. Moreover, the SCF provides information on various household socio-economic characteristics and

⁸SCF only omits the Forbes 400 for confidentiality reasons. By contrast, the Panel Study of Income Dynamics does not oversample the wealthy nor does it provide a disaggregation of different stockholding modes.

saving attitudes that we control for in our analysis. On the other hand, we note that the SCF does not allow calculation of a credible measure of the present value of pension wealth in defined benefit plans. As a result, our analysis cannot assess directly the implications for wealth levels and inequality of the considerable shift from defined benefit to defined contribution plans and individual retirement accounts observed in this period.

In what follows, we use data from 1989, 1998, and 2001 SCF surveys. The 1989 SCF is the first survey that provides all responses used in our analysis (e.g. on saving attitudes) in a manner comparable to the subsequent surveys. The period covered by our data allows us to study most of the growth in stock market participation and the underlying transformation of the stockholding pool through a substantial stock market upswing followed by a downswing. ¹⁰

Specifically, this period witnessed a general increase in stock market prices between the 1989 and 1998 surveys, and a subsequent burst of the Internet bubble prior to the 2001 survey. As our aim is to uncover the link between stockholding behavior and the distribution of wealth, we focus on a period exhibiting important stock market developments, and we do not extend the analysis to the subsequent financial crisis and the Great Recession. Unlike the period we consider, the subprime crisis emanated in a real rather than in a financial asset, was strongly linked to collateral values and debt behavior, and was accompanied by considerable increases in unemployment. Indeed, recent work (e.g. Demyanyk *et al.*, 2015) finds that the relationship between the behavior of consumers and key economic variables was very different across these crises. We provide details on the data, asset categories, and variable definitions in a Data Appendix, available from the authors on request.

Existing household finance literature shows consistently that certain characteristics make it more likely that a particular household will be drawn into the stockholder pool. We report in Table 1 marginal effects from probit regressions, for each of the three survey years, that control for a similar array of demographic and pecuniary characteristics to that employed in relevant studies (see, for example, the empirical contributions in Guiso, Haliassos, and Jappelli, 2001). Consistent with existing literature, we find that being affluent, more educated, and less risk averse contribute to the probability of owning stocks (held directly and indirectly), controlling for other factors. These results imply that certain characteristics contribute to the probability of being a stockholder, and that the composition of the stockholder pool changes in general as stock market participation

⁹Calculating the present value of future income streams from defined benefit plans requires several assumptions ranging from future events and work decisions to discount rates and mortality (for more details, see, e.g. Aizcorbe, Kennickell, and Moore, 2003).

¹⁰It should be noted that our analysis does not cover the entire increase in stock market participation given that part of it has taken place prior to 1989 (according to the 1983 SCF only 19 percent of households were classified as stock holders).

¹¹All monetary values have been deflated and are expressed in constant 2004 U.S. dollars. In this paper, we try to avoid some pitfalls involved in automatic computation of marginal effects by standard econometric software, which have recently been emphasized (see Appendix A).

¹²Receiving an inheritance is also strongly related to stock ownership, consistent with the Investment Company Institute and Securities Industry Association study entitled "Equity Ownership in America," which reports that of equity holders surveyed "more than one fifth own individual stock portfolios received as gifts or inheritances".

TABLE 1
PROBIT REGRESSIONS FOR OWNERSHIP OF EQUITY HOLDINGS

	1989		1998		2001	
	Marginal Effect	t-value	Marginal Effect	t-value	Marginal Effect	t-value
Age	0.0031***	4.62	0.0027***	4.60	9000.0	0.91
Male	0.0097	0.33	0.0041	0.17	0.0346	1.41
Married	0.0720***	2.81	0.0985***	4.25	0.0645***	3.15
Has children	-0.0395**	-2.23	-0.0255*	-1.69	-0.0086	-0.57
White	0.1244***	5.89	0.1412***	7.73	0.1166***	6.47
Health poor	-0.1287***	-4.06	**96/0.0-	-2.25	-0.1849***	-5.55
High school graduate	0.1556***	98.9	0.1918***	8.03	0.1969***	8.25
College graduate	0.2867***	11.27	0.3437***	13.11	0.3638***	14.05
Save for "rainy days"	-0.0050	-0.32	-0.0026	-0.18	-0.0049	-0.32
Credit constrained	-0.0407*	-1.68	-0.0086	-0.49	-0.0476**	-2.44
Non-investment Income	0.0076***	5.99	***9800.0	6.92	0.0071***	7.00
Non-equity net total Wealth	0.0116***	7.11	0.0088**	7.54	0.0087***	7.68
Expect to leave a bequest	0.0784***	4.65	0.1144***	7.84	0.1128***	7.98
Has received inheritance	0.0292*	1.77	0.0697***	4.17	0.0489***	2.64
Financial alertness	-0.0197	-1.20	0.0239	I.2I	0.0177	1.06
Willingness to take above average financial risk	0.0809***	3.89	0.1871***	11.75	0.1701***	10.34
Investment horizon > 10yrs	0.0481**	2.44	0.1076***	4.96	0.0486***	2.65
observations	3143		4305		4442	
log likelihood	-1530.8		-1982.8		-1970.2	

Data from Surveys of Consumer Finances. The specification accounts for age through a 2nd order polynomial, and for labor status. It controls for income, and non equity net total wealth using the inverse hyperbolic sine transformation: $\log(x + (\tilde{x}^2 + 1)^{1/2})$. Marginal effects are averaged across households (using survey weights). The marginal effects for income and non equity net total wealth are based on a \$5000 increase in the underlying variables and for age on a one year increase. Numbers in italies report t-values, derived from simulated standard errors (details can be found in appendix A). ***, ** and *denote significance at 1%, 5% and 10% level, respectively. Reported estimates are corrected for multiple imputation.

TABLE 2

EDUCATIONAL ATTAINMENT, INCOME AND NET WEALTH IN THE POPULATION AND AMONG EQUITY OWNERS

	1989	1998	2001
Population			
Education (%)			
Less than high school education	23.3	15.4	15.2
High school graduates	48.8	51.4	50.9
College degree or more	27.9	33.2	33.9
Mean (Median) non-investment Income	51,203	56,538	64,102
	(35,168)	(37,245)	(38,691)
Mean (Median) non-equity Net total Wealth	249,749	244,506	308,318
* * *	(66,469)	(68,579)	(76,679)
Equity Owners (%)	31.8	48.9	51.9
Equity Owners			
Education (%)			
Less than high school education	7.3	5.4	4.7
High school graduates	45.5	47.8	45.7
College degree or more	47.2	46.8	49.6
Mean (Median) non-investment Income	87,145	82,825	93,731
•	(61,161)	(58,783)	(61,091)
Mean (Median) non-equity net total Wealth	513,993	390,595	486,494
* V	(181,918)	(127,400)	(154,720)

Weighted data from Surveys of Consumer Finances. The reported statistics are corrected for multiple imputation. The sample of equity owners includes households who own directly or indirectly stocks. Money values refer to 2004 Dollars.

spreads. Yet, it is not clear whether observed differences in stock investing over time are due to changes in the composition of the U.S. stockholder pool, e.g. in terms of characteristics, or are due to changes in the systematic relationship of these characteristics to stockholding levels. We attempt to address this issue using counterfactual analysis and discuss the results in the next section.

In Table 2 we present summary statistics on three factors often considered as key for stock investments, namely education, income and (non-equity) net wealth. These statistics show notable changes in the composition of the stockholder pool, as it was expanding, both in absolute terms and relative to the population. While they do suggest an increase in the share of "small" and less educated stockholders during the upswing, they fail to indicate a continuation of this trend through the downswing. Specifically, by 1998 the share of college graduates among equity holders was somewhat reduced to 46.8 percent, while in the population it increased by almost 6 percentage points. This suggests that, in 1998, the stockholder pool was not enriched with more educated investors to the same extent as the general population. In addition, both the mean and median non-investment income among equity holders is lower in 1998 compared to 1989, while

¹³In all regression specifications of ownership or amounts invested in stocks, we control for net wealth after deducting the amount invested in equity (in any form) in order to minimize endogeneity problems. For consistency, we report summary statistics with reference to this measure (i.e. non-equity net wealth). As already discussed, the measure of net wealth does not incorporate the present value of defined benefit plans because of data limitations.

in the population it is considerably higher, by 10 percent and 6 percent, respectively. A similar picture emerges when we look at net wealth.

However, by 2001 college graduates among equity holders reach 49.6 percent, an increase of almost 3 percentage points within just three years, while their population share remains unchanged. They also show significant increases at all percentiles of income and wealth distribution (for instance, median non equity net worth increased two times more among equity holders compared to the population). If anything, summary statistics suggest that the composition of stockholders shifted against "small" investors during the downswing, despite increased participation.

2.1. The Composition of the Stockholder Pool: Counterfactual Distributions

Changes over time across the entire distribution of stockholding levels result partly from changes in the configuration of stockholder attributes and partly from changes in the value of holdings among households of a given configuration of characteristics. The latter can be mainly linked to the prevailing economic environment, including the level of the stock market prices in a given year or increased availability of defined contribution pension plans. Summary statistics or regression estimates of isolated household characteristics are not sufficient to distinguish the combined contribution of various characteristics to stockholding levels from that of the prevailing economic environment.

We use recent advances in counterfactual distributions to decompose observed changes in equity holdings into those arising from changes in the economic environment facing stockholders of given characteristics; and those resulting from changes in configuration of characteristics of the stockholder pool, as participation spreads. While the stock market went up and down during the entire period and it is natural for changes in market valuation to have affected equity holdings of stockholders with given characteristics, we are interested in seeing whether changes in the composition of the pool also contributed to observed changes in the distribution of equity holdings, from large to small, and in which direction.

We apply a variant of the counterfactual decomposition technique proposed by Machado and Mata (2005), described in Appendix B. We run a series of quantile regressions¹⁵ and we decompose the change in the distribution of equity holdings between two years into (i) a component due to changes in the *coefficients* on given stockholder characteristics at various percentiles of the stockholding distribution; and (ii) a component due to the change in the distribution of *covariates*, i.e. configuration of stockholder characteristics.

¹⁴Such techniques have been broadly used in the labor literature to decompose observed changes in the income distribution into changes in labor market conditions and changes in characteristics of the labor force. For a recent study on trends in U.S. wage inequality in the last 40 years see Autor, Katz, and Kearney (2008). Christelis, Georgarakos, and Haliassos (2013) have used these techniques to decompose differences in household portfolios between two countries into differences in characteristics and differences in economic environments faced by households of similar characteristics that live in different countries.

¹⁵Regressors are the same as for the participation probits, presented in Table 1.

When comparing two different years, say 1998 to 1989, the relevant counterfactual distribution is the (logarithm of) equity holdings that stockholders in 1989 would have if they had experienced the same economic environment faced by stockholders in 1998. Formally, the difference between the 1998 and 1989 distributions of equity holdings at each percentile is decomposed into:

(1)
$$f(y^{98}) - f(y^{89}) = \{f(y^{98}) - f^*(y; X^{89}b^{98})\} + \{f^*(y; X^{89}b^{98}) - f(y^{89})\}$$

where y represents the log of equity wealth, X is the data matrix and b is a vector of estimated quantile regression coefficients evaluated at various percentiles. The difference in the first curly brackets represents the contribution of household characteristics to the overall difference between the 1998 and 1989 distributions of equity holdings ("covariate effects") for given economic environment. The difference in the second curly brackets measures the contribution of differences in economic environment facing households of given characteristics ("coefficient effects").

Coefficient and covariate effects for 1998–1989 are presented in Figure 1a and are statistically significant across percentiles, based on bootstrapped standard errors not reported here. Differences in distributions of equity holdings over this period are mainly driven by coefficient effects, and these become progressively more important at higher percentiles of the distribution. This is consistent with the exceptionally strong upward movement of stock market indices over this period, that allowed owners of given characteristics to exhibit much larger stock holdings in 1998 compared to 1989.

On the other hand, covariate effects are negative, implying that the 1989 stockholder pool would have generated even higher equity holdings under the 1998 economic environment than those that were actually observed among 1998

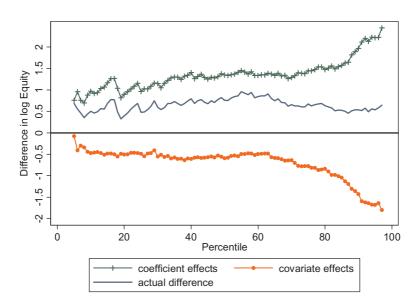


Figure 1A. Quantile Regression Decomposition 1998–1989: Coefficient and Covariate effects

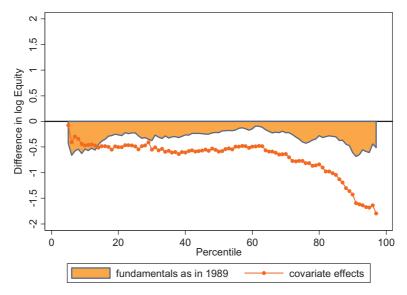


Figure 1B. Quantile Regression Decomposition 1998–1989: Contributions of Fundamentals to Covariate effects

stockholders. In other words, the distribution of characteristics in the wider stockholder base at the end of the 1990s was not as conducive to high equity levels as the 1989 distribution.

Comparisons of 1989 to 1998, the last period during the upswing for which SCF data are available, are consistent with the conjecture that the stockholder base underwent progressive dilution with smaller stockholders as participation grew during the upswing. However, when we compare 1998 with 2001, a period encompassing the stock market downturn, findings are reversed (Figure 2a). The decomposition is:

$$(2) f(y^{2001}) - f(y^{98}) = \{f(y^{2001}) - f^*(y; X^{2001}b^{98})\} + \{f^*(y; X^{2001}b^{98}) - f(y^{98})\}$$

We find that coefficient effects are negative, as expected due to the decreased value of stocks following the downswing. However, covariate effects on equity holdings (displayed in the second curly brackets) are positive and increasing beyond the 40th percentile of the distribution of stock wealth. ¹⁶ This implies that a stockholder pool with the configuration of stockholder characteristics of 2001 would have had higher equity levels in 1998, compared to those actually observed for 1998 stockholders. In turn, this suggests a tilt in the configuration of the stockholder pool towards larger holdings between 1998 and 2001, accompanying the continuing increase in participation.

These, combined with our findings for 1989–1998, point to the conclusion that the composition of the stockholder pool changed considerably with stock market

¹⁶Both coefficient and covariate effects are statistically significant at percentiles above the 25th according to (non-reported) bootstrapped standard errors.

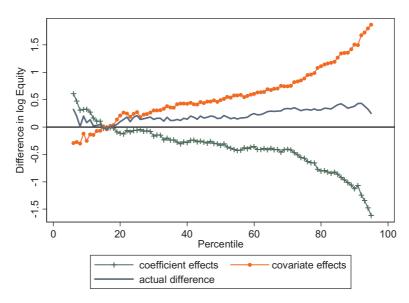


Figure 2A. Quantile Regression Decomposition 2001-1998: Coefficient and Covariate Effects

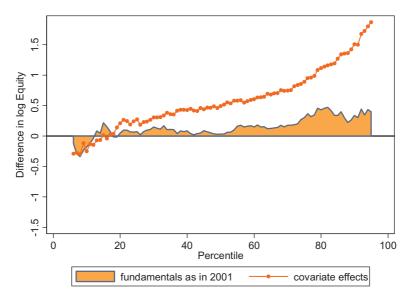


Figure 2B. Quantile Regression Decomposition 2001–1998: Contributions of Fundamentals to Covariate Effects

conditions: during stock market upswings, the stockholder pool became more conducive to smaller holdings, but during downswings the balance was tilted towards bigger holdings, presumably by attracting predominantly larger investors and losing smaller ones. While the cross-sectional nature of SCF does not allow us to observe entries and exits directly, recent work by Bilias, Georgarakos, and

Haliassos (2010) using panel data from the PSID and different techniques confirms that exits occurred despite the overall increase in participation, and that factors significantly contributing to exits included lower resources (income, non-stock net financial wealth, or net real wealth) and minority status, in good and in bad times; and poor health in bad times.

2.2. A Role for Financial Attitudes and Practices?

So far, we have used the terms "large" or "small" investor merely with reference to their likely level of stockholding, but without asking whether this level can be traced partly to a subset of characteristics that relates to financial attitudes and practices. This issue is relevant for understanding the implications of increased reliance on household decision making for managing riskier portfolios and providing for retirement.

We extend our counterfactual analysis in order to estimate the contribution of changes in configurations of financial attitudes and practices within the stockholder pool. We are conservative in what we include under attitudes and practices, in that we do not include factors such as education, which helps shape attitudes and inform practices but also determines the income process faced by the household. In this sense, we are likelyif anything—to underestimate the quantitative importance of financial attitudes and practices. We consider three factors, namely risk attitudes proxied by reported willingness to take more than average risk; reporting a long investment horizon (in excess of 10 years); and "financial alertness" (defined as shopping around extensively for the best terms before making major borrowing and saving decisions).

We perform the following sequential decomposition:

(3)
$$f(y^{98}) - f(y^{89}) = \{f(y^{98}) - f^{**}(y; X_f^{98}, X_a^{89}, b^{98})\} + \{f^{**}(y; X_f^{98}, X_a^{89}, b^{98}) - f^{*}(y; X^{89}b^{98})\} + \{f^{*}(y; X^{89}b^{98}) - f(y^{89})\}$$

where the counterfactual f^{**} represents the equity wealth distribution that would have prevailed in 1998 if the configuration of financial attitudes in the stockholder pool were distributed as in 1989. The term in the second curly bracket shows the relative contribution of other household characteristics.

Figure 1b exhibits this decomposition of covariate effects for the 1989 to 1998 period. The blank area represents the effects of changes in financial attitudes and practices and implies a considerable contribution throughout the distribution of equity holdings.

Figure 2b carries out an analogous exercise for the period between 1998 and 2001. Here we use the following sequential decomposition:

(4)
$$f(y^{2001}) - f(y^{98}) = \{f(y^{2001}) - f^*(y; X^{2001}b^{98})\} + \{f^*(y; X^{2001}b^{98}) - f^{**}(y; X_f^{98}, X_a^{2001}, b^{98})\} + \{f^{**}(y; X_f^{98}, X_a^{2001}, b^{98}) - f(y^{98})\}$$

Results are quite similar, with greater room for effects of attitudes above roughly the 70th percentile of the distribution of equity holdings.

Thus, counterfactual analysis suggests that the period 1989–1998 has witnessed a tilt of the stockholder base towards smaller holdings, partly because of financial attitudes and practices. The subsequent, 1998–2001 period is even more interesting, as it seems to combine a shift in the composition of characteristics, attitudes and practices of the stockholder base towards larger holdings despite the continuing increase in overall participation. To put it differently, our findings suggest that the stock market downswing has had a "cleansing effect" on the characteristics, attitudes, and practices of the stockholder pool.¹⁷

3. How Important is Stockholding for Net Wealth Inequality?

In this Section, we document changes in inequality of net total wealth among U.S. households between 1989 and 2001 and investigate the importance of stockholding for these changes. ¹⁸ The first subsection computes net wealth inequality indices to show that different parts of the distribution of net wealth have been affected quite differently over this period, rendering blanket statements about net wealth inequality misleading. The second subsection presents inequality decompositions by asset components to show that, despite the rich pattern of inequality changes, stock investing has become dramatically more important for net wealth inequality regardless of whether we focus mainly on inequality at the upper end or in the middle of the distribution.

3.1. How has Net Wealth Inequality Changed?

As discussed, data from SCF are particularly well suited for analysis of the wealth distribution, given that they over-sample the rich and they are not subject to top-coding of wealthy households carried out in other surveys. It should be noted that the presence of the rich is very important in studying the wealth distribution and inequality since the richest 1 percent of households possesses roughly the 1/3 of the total wealth (see Kennickell, 2003).

We first compute four commonly used measures of inequality, which are sensitive to changes in different parts of the distribution¹⁹ Mean logarithmic deviation (MLD), Theil, Half of Squared Coefficient of Variation (HSCV), and Gini. Theil's index is influenced by the relative distance between the rich and the poor, attaching more weight to transfers at the lower and upper ends. HSCV is very

¹⁹As Atkinson (1983) points out, "[inequality indices] embody implicit judgments about the weight to be attached to the inequality at different points in the [...] scale". Details on the asset definitions are available from the authors on request. Formulae for inequality indices are provided in Appendix C.

¹⁷As noted above, this was partly accomplished through exits of smaller investors. It may have also been helped by improvements in the financial attitudes and practices of some investors who remained in the market following the downswing.

¹⁸The measurement part of our analysis of wealth distribution is complementary to the careful work by Kennickell (2003), which is based on the same set of SCF surveys. Kopczuk and Saez (2003) use estate tax returns to study shares of wealth held by the very rich and they find, consistent with Kennickell, that top wealth shares have not increased since 1995, and that the share of stock market wealth held by the richest (relative to the total stock market wealth held by the whole population) fell in the past 20 years. They attribute the latter finding partly to increased stock market participation.

TABLE 3

NET WEALTH INEQUALITY INDICES

	Gene	eralized Entropy	Class	
Year	GE(0) MLD	GE(1) Theil	GE(2) HSCV	Gini
1989 1998 2001	2.022 1.860 1.966	1.523 1.646 1.622	14.037 19.156 12.847	0.769 0.776 0.788

Weighted data from Surveys of Consumer Finances. The reported statistics are corrected for multiple imputation. The sample excludes households with negative net worth.

sensitive to changes in the upper tail of the distribution: it is very sensitive to inequality at high wealth levels but less so to inequality at other regions of the distribution (Cowell, 1977; Shorrocks, 1980). Gini is more sensitive to the middle of the distribution.

Table 3 reports computed values of four inequality indices for net overall wealth in 1989, 1998, and 2001. MLD records a sizeable decrease in inequality between 1989 and 1998, followed by an increase to a level in 2001 that falls short of inequality at the starting point. Theil and HSCV record increased inequality in 1998 compared to 1989, followed by a reduction in inequality between 1998 and 2001. Finally, Gini records a slight increase in net wealth inequality over time.

The patterns we observe, especially the movements in HSCV and Theil, suggest that net wealth inequality at the upper end of the wealth distribution increased during the stock market upswing and the spread of defined contribution pension plans of the 1990s and diminished during the subsequent downturn. The increase in the Gini coefficient suggests some increase in inequality among middle net-wealth classes throughout the period under examination.

3.2. The Growth in Importance of Stockholding for Net Wealth Inequality

Appropriate decompositions of inequality indices allow us to investigate the relative importance of different asset components of net total wealth for generating inequality at different points in the distribution. Inequality in a variable W in a given year, I_W , can be expressed as an exact sum of the contributions made by its various factor components:

$$I_W = \sum_f S_f$$

A factor component contributes to increased (reduced) inequality if $S_f > 0$ (<0). The share of a particular factor f, s_f , in generating inequality is defined as: $s_f = \frac{S_f}{I_W}$, and thus: $\sum_f s_f = 1$. In what follows, we focus on the top of the net wealth distribution (which accounts for the main bulk of equity holdings) using the HSCV

²⁰Inequality indices for gross total wealth over the full sample of households produce a similar picture.

as well as on the middle of the distribution using the Gini. Despite their recorded differences, decompositions of both measures point to the substantial growth in importance of stockholding for net wealth inequality.

3.2.1 Decomposition of HSCV by Source

HSCV has desirable decomposability properties and it can handle the regular incidence of zero asset holdings.²¹ Appendix C provides details on the exact decomposition of HSCV into the factor components reported in Table 4.

Table 4 shows decompositions of inequality by source, as measured by HSCV.²² Stock holdings are not the dominant source of net wealth inequality, but neither is primary residence that forms the biggest part of most households' portfolio. Indeed, wealth in primary residence has a much smaller effect on net wealth inequality than stockholding, and one not consistent with the overall trend.

The factor with the greatest proportional contribution to net wealth inequality is risky real assets (business equity and investment real estate excluding primary residence), which make a more than 50 percent contribution in all three years (1989, 1998, 2001). Yet ownership rates of risky real assets do not exhibit any strong trend between 1989 and 2001, hovering around 27 percent. Risky real assets exhibit high degree of inequality and high correlation with overall net wealth, but in 1998, the year that overall inequality spikes by the HSCV measure, the absolute factor contribution of risky real assets and business equity increases only slightly (from 10.16 to 11.63).²³ Given the much higher increase in net total wealth inequality, the proportionate factor contribution actually drops (from 0.72 to 0.60).

Stock holdings, on the other hand, represent the factor with the biggest growth in importance and they exhibit changes in inequality consistent with those of net wealth. By 1998, wealth in equity holdings accounts for more than 25 percent of net total wealth inequality, compared to just 7 percent a decade before.²⁴ Directly and indirectly held equity plays the dominant role in the *increase* of overall net wealth inequality by 1998, based on the percentage change in source contributions. Between 1998 and 2001, the reduction in inequality of equity holdings (attributable mainly to the significant reduction in inequality among equity holders but also to the higher percentage of owners) more than outweighs the increase in their relative correlation and share, contributing to a fall in net total wealth inequality. However, their proportionate contribution to net wealth inequality remains at 25 percent. One may wonder whether these conclusions on

²¹See Jenkins (1995) for a similar argument in favor of using HSCV for analysis of income inequality.

²²Decompositions presented in tables 2 and 3 have been also applied to gross total wealth using the full sample of households and excluding the two categories that represent debt. In all cases they suggest similar patterns to those we present.

²³This is because the dropping factor share and correlation with net total wealth moderate the effects from the increase in this factor's inequality.

²⁴Stock holdings exhibit a high increase in factor share, increased correlation with net total wealth, and increased inequality (coming from the increase in within inequality that almost doubles, outweighing the effect from the increase in the percentage of stock owners), all leading to a more than quadruple increase in their absolute factor contribution between 1989 and 1998.

TABLE 4

Net Wealth Inequality Decomposition by Sources Using HSCV

			,						
	Year	Net Total Wealth	Wealth in Safe Financial Assets	Wealth in Equity Holdings	Net Wealth in Risky Real Assets and Bus. Equity	Other Wealth	Wealth in Primary Residence	Principal Residence Debt	Consumer Debts
Percentage with positive factor wealth (n_f^+)	1989 1998 2001	0.957 0.973 0.973	0.907 0.936 0.937	0.339 0.512 0.537	0.289 0.271 0.259	0.857 0.850 0.870	0.681 0.703 0.714	0.418 0.454 0.468	0.615 0.607 0.616
Factor Share (χ,)	1989 1998 2001	1.000	0.251 0.219 0.212	0.100 0.254 0.268	0.353 0.296 0.287	0.061 0.054 0.048	0.356 0.320 0.307	-0.093 -0.115 -0.102	-0.029 -0.029 -0.022
Correlation with net total wealth (ρ_{JW})	1989 1998 2001	1.000	0.542 0.559 0.639	0.446 0.647 0.682	0.905 0.863 0.825	0.267 0.358 0.370	0.401 0.401 0.507	-0.174 -0.160 -0.183	-0.264 -0.358 -0.203
Factor Inequality (L _f)	1989 1998 2001	14.037 19.156 12.847	16.831 14.592 18.211	37.110 46.750 24.825	72.197 108.032 63.960	31.696 7.909 8.038	1.362 1.376 1.561	2.351 1.696 1.836	11.891 26.424 22.817
Within Factor Inequality $egin{pmatrix} \Gamma_f \end{pmatrix}$	1989 1998 2001	13.409 18.628 12.462	15.226 13.631 17.036	12.257 23.695 13.106	20.257 28.881 16.178	27.318 6.649 6.932	0.767 0.819 0.971	0.692 0.498 0.592	7.126 15.851 13.857
Proportionate Factors contributions (s_{j})	1989	1.000	0.149	0.073	0.722 0.606	0.025	0.045	-0.007 -0.005	-0.007 -0.012
Absolute Factors contributions (S _j)	2001 1989 1998 2001	14.037 19.156 12.847	2.082 2.082 2.045 2.074	1.013 4.918 3.262	10.163 11.634 6.797	0.346 0.237 0.182	0.622 0.657 0.698	-0.093 -0.104 -0.090	-0.098 -0.230 -0.076
Percentage change in source contributions (s/%\DS_f)	1998–1989 2001–1998	0.365	-0.003 0.002	0.280	$0.105 \\ -0.252$	-0.008	0.003	-0.001	-0.009

Weighted data from Surveys of Consumer Finances. Factor inequality reports the HSCV for the respective asset category calculated over the entire sample. Within factor inequality reports the HSCV for the respective asset category calculated over the sub-sample of owners of this asset. The reported statistics are corrected for multiple imputation. The sample excludes households with negative net worth.

the importance of stockholding depend on using HSCV, which is sensitive to the upper tail of the distribution. The next subsection examines robustness with respect to using the Gini index.

3.2.2 Decomposition of the Gini Index by Source

Despite the fact that the Gini coefficient focuses on the middle of the distribution and records increased inequality throughout the period under study, Gini decompositions reinforce the conclusions based on HSCV.

Table 5 reports decompositions of inequality of net total wealth as summarized by the Gini coefficient (see Appendix C for explanation of the exact decomposition). Equity holdings display one of the highest rank correlation ratios, which gets higher over time, highlighting the growing importance of risky financial assets for households' position in the overall net wealth distribution. In the period 1989–1998, stock holdings represent the only wealth component that contributes to the rise in net wealth inequality (i.e. there is an increase in both the absolute and proportionate contributions of stock holdings to net wealth inequality, despite that the Gini for stocks has somewhat declined from 0.939 to 0.908). The main factor behind this increased contribution is the rise in the share of stock holdings in net total wealth over this period (i.e. from 0.10 to 0.25). This arose mainly from the spread of participation to more households and the increases in valuation during the upswing.

All in all, we do not find that either stock wealth or net overall wealth inequality fell consistently through the period of sustained increase in stock market participation. Net wealth inequality has followed the same pattern as stock wealth inequality over the period and stock wealth inequality has grown in importance significantly as a component of net wealth inequality.

4. CONCLUDING REMARKS

Household participation in stockholding grew dramatically in the U.S. in the face of the stock market upswing and spread of defined contribution pension plans during the 1990s, and of the subsequent downswing in the early 2000s. In this paper, we have employed high-quality household-level data from the SCF to shed light on the important links between increased participation in stockholding, changing characteristics of the stockholding pool, and net wealth inequality.

We used counterfactual decomposition techniques in order to attribute changes in stock investing in two points in time into a part that is due to changes in the economic environment and another part that is due to changes in the configuration of characteristics of the stockholder pool. Our results imply that the share of smaller stockholders increased during the booming stock market of the 1990s, while the subsequent downturn improved the tendency of the stockholder pool to exhibit large equity holdings. In this sense, the U.S. experience between 1989 and 2001 seems consistent with a "dilution effect" during the stock market boom, followed by a "cleansing effect" of the stock market downturn. Our findings support the view that heterogeneity in household characteristics, as well as financial attitudes and practices, matter for stockholding levels.

 ${\bf TABLE} \; {\bf 5}$ Net Wealth Inequality Decomposition by Sources Using Gini

			-	;	Net Wealth in		Wealth in	Principal	
	Year	Net Total Wealth	Wealth in Safe Financial Assets	Wealth in Equity Holdings	Risky Real Assets and Bus. Equity	Other Wealth	Primary Residence	Residence Debt	Consumer Debts
Factor Share (χ_{ρ})	1989	1.000	0.251	0.100	0.353	0.061	0.356	-0.093	-0.029
	2001	1.000	0.212	0.268	0.287	0.048	0.307	-0.102	-0.022
Rank correlation ratio (R _{fW})	1989	1.000	0.913	0.909	0.942	0.729	0.821	0.445	0.385
	1998	1.000	0.902	0.932	0.945	0.654	0.812	0.443	0.329
	2001	1.000	0.914	0.939	0.948	0.692	0.841	0.473	0.299
Gini Index (G_f)	1989	0.769	0.823	0.939	0.957	0.664	0.645	0.795	0.784
	1998	0.776	0.809	0.908	0.955	0.618	0.605	0.749	0.794
	2001	0.788	0.831	0.898	0.955	0.601	0.624	0.750	0.776
Proportionate Factors	1989	1.000	0.245	0.1111	0.414	0.039	0.245	-0.043	-0.011
contributions (s_f)	1998	1.000	0.206	0.277	0.345	0.028	0.202	-0.049	-0.010
	2001	1.000	0.205	0.287	0.330	0.026	0.205	-0.046	-0.006
Absolute Factors	1989	0.769	0.189	0.085	0.318	0.030	0.189	-0.033	-0.009
contributions (S_{ℓ})	1998	0.776	0.160	0.215	0.267	0.022	0.157	-0.038	-0.007
	2001	0.788	0.161	0.226	0.260	0.020	0.162	-0.036	-0.005

Weighted data from Surveys of Consumer Finances. The reported statistics are corrected for multiple imputation. The sample excludes households with negative net worth.

We found inequality in equity holdings to be quite important for inequality in overall net wealth, despite their limited share in net wealth. However, our findings suggest that reduced wealth inequality is far from being an automatic outcome of the spread of stock market participation. The distributions of stock holding and net wealth levels are significantly related to household characteristics and to their financial attitudes and practices. By highlighting the relevance of such factors for net wealth inequality, our findings contribute to the debate on the importance of financial education, advice, and well-designed default options, as responsibility for retirement financing is shifted from Social Security to households, challenging disproportionately the small and less sophisticated investors.

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SUPPORTING INFORMATION

Additional Supporting Information may be found in the online version of this article at the publisher's web-site:

- Appendix A: Simulated Average Marginal Effects
- Appendix B: The Machado-Mata Algorithm
- Appendix C: Formulae for Inequality Indices and Their Decompositions