

Review of Income and Wealth Series 60, Number 3, September 2014 DOI: 10.1111/roiw.12106

PENSIONS FOR SINGLES AND COUPLES

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Retirement policies often seek to set pensions at levels that enable single and married pensioners to have the same standard of living. The existing literature on consumer equivalence scales provides little assistance in reaching this policy objective, as the estimated scales are both imprecise and reliant upon strong and opaque assumptions. This paper proposes an alternative modeling strategy which has low data requirements and involves the use of detailed, but transparent, assumptions about the extent of joint consumption of particular commodities. These assumptions are embedded in an economic model of household consumption and combined with household expenditure data to calculate consumer equivalence scales. It is estimated that, in 2003–04, Australian couples of Age Pension age who owned their own home needed expenditures between 1.32 and 1.60 times that of a single person. These scales were lower than those used in the pension system.

JEL Codes: D13, I38, J14

Keywords: consumer equivalence scales, pensions

INTRODUCTION

Retirement policies often seek to set minimum pensions at levels that enable single and married pensioners to have the same standard of living. Information about relative needs is also needed for poverty and inequality measurement. Seemingly, data on household consumption patterns should be able to inform these applications. However, consumption research typically plays little part in the setting of pension relativities, and has a very limited input into poverty and inequality measurement. Research-based relativities with useful levels of precision both require very strong and opaque assumptions and/or have very high data requirements.

This paper introduces a modeling framework that can be used when deriving such "consumer equivalence scales." It is set in the context of consumer demand theory and uses data on consumer expenditure patterns, but also draws upon systematically assembled assumptions about the joint consumption of commodities in the household. These assumptions are akin to, but weaker than those used in the normative "budget standards" literature. The key strengths of the method

Note: This research was supported by the Australian Government Department of Families, Housing, Community Services and Indigenous Affairs (FaHCSIA) and by the Australian Research Council (DP0878643). The opinions, comments, and/or analysis expressed in this document are those of the author and do not necessarily represent the views of the Minister for Families, Housing, Community Services and Indigenous Affairs or FaHCSIA, and cannot be taken in any way as expressions of Government policy. Research assistance from Silvia Mendolia and comments from Peter Saunders, seminar participants, and two anonymous referees are gratefully acknowledged.

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are that data requirements are low and the assumptions used are quite transparent. The key weakness is that assumptions (or external evidence on the technology of home consumption) are required. Nonetheless, the clear link between assumptions and conclusions used in this framework means that it can be used to provide a key input into normative pension policy (and possibly also for related distributional research). This framework is applied to estimate the relative needs of singles and couples of Age Pension age in Australia.

The Australian Age Pension is a non-contributory pension paid to around three-quarters of the population over retirement age (high-income or wealthy people are excluded). Prior to September 2009, the Australian Age Pension had a base rate of payment for a couple that was 1.64 times the single rate of pension.¹ For several years, Australian seniors groups had been campaigning to seek increases in the relative payments for single pensioners.² Moreover, the couple/ single ratio was higher than many equivalence scales in common use in poverty research. In their 1988 survey, Buhmann *et al.* found that scales based on subjective evaluations of well-being had very high economies of scale (median couple/ single ratio of 1.18), while scales based on expenditure patterns or derived from official poverty lines had economies of scale averaging 1.32 and 1.42, respectively. (Though it should be noted that these summary statistics are averaged across all family sizes, and not specifically developed for the comparison of singles and couples.) Only scales arbitrarily created by statistical agencies or researchers had similar scale economies to the Australian pension scale relativity.

These different approaches are considered in more detail in the next section of the paper. The method used here includes elements of both the consumption theory and the normative "budget standards" approach. The "Barten" model used in this paper is introduced in Section 2. The calculation methods used in this paper do not require the estimation of a full consumer demand system, but instead are based on price index-like weighted averages of budget shares. The implications of using the Barten simplifications are discussed with reference to a more general household consumption model which is outlined in the Appendix. Section 3 then provides estimates of the relative needs of Australian older couples and singles who own their own homes. A number of extensions to these estimates are presented in Section 4. These include estimates of the impact of age on the relativity between singles and couples, the relative needs of single and couple private renters, and the relative needs of two-person, non-couple households. Section 5 concludes.

1. EQUIVALENCE SCALE ESTIMATION

There is a longstanding debate in the economics literature on whether the consumer equivalence scale is a meaningful concept. If people can choose their

¹This is for home-owners and includes utility, telephone, and pharmaceutical allowances. As a comparison, the couple/single ratio in the U.K. Basic State Pension is 1.60 when only one member of the couple has qualifying National Insurance contributions (www.direct.gov.uk; accessed August 5, 2010).

 $^{^{2}}$ Yates (2009, p. 1). See also Barber *et al.* (1994) and Patterson and Wolffs (1995) who presented anecdotal and focus group evidence about the perceived drop in living standards experienced by pensioners after the death of their partner.

family size, then it makes little sense to assume that they are worse off when they make a choice to have a larger (or smaller) family.³ Why should we be interested in estimating the costs but not the benefits associated with household structure, and why should income transfer programs take account of these costs?

One reason is that researchers and policy-makers are often interested in the living standards of people who have little choice over their living arrangements. This is relevant when considering the living standards of children, who do not choose to be brought into the world nor the number of siblings they have. It might also be considered relevant to the situation of the majority of older singles, because they have arrived in this situation via widowhood.

More generally, we might wish to apply social norms that are not automatically derived from individual behavior.⁴ These might include the right of individuals to choose their demographic status without incurring economic penalties. For example, a goal of pension policy for the elderly might be to permit both singles and couples to live in their preferred household composition while attaining the same material standard of living. Similarly, social goals of poverty alleviation are usually defined within the narrower context of commodity-based consumption—partly because economic and social policy is not very effective in altering demographic choices or providing the benefits (such as companionship) that flow directly from household composition. Hence anti-poverty policy seeks to take consumer equivalence scales into account in setting rates of payment (Nelson, 1993; Bradbury, 2003). This focus on commodity consumption is also a justification for ignoring the leisure and home production costs and benefits of various domestic arrangements.

Within this narrower framework of consumption-based welfare, there is a large and longstanding body of research seeking to measure the relative needs of families of different compositions (surveyed in Buhmann *et al.*, 1988). The methods used can be grouped into three broad categories based on their most important identifying assumptions.

Well-Being Indicator Based

Subjective measures of economic well-being or hardship can be compared with income levels to ascertain the income level needed to maintain constant well-being across different household types (e.g., Kapteyn and Wansbeek, 1985). This controls for the different income levels of people in different household types.

The validity of this approach rests on the assumption that responses to these questions accurately reflect the concept of well-being that is of interest to researchers. This might not be the case, for example, if subjective well-being is influenced by expectations, particularly if these in turn are influenced by the living standards of people in other households of the same type as the respondent. If this is the case,

³See, for example, Pollak and Wales (1979) and Blundell and Lewbel (1991). The latter conclude that to use equivalence scales derived from demand data for welfare comparisons is "inherently dishonest or at least uninformative" (p. 66). This present paper argues that, contrariwise, the types of scale estimated here are very informative for the narrower questions of relevance to pension policy.

⁴That is, social welfare functions may have a more restricted set of arguments than individual welfare functions, excluding preferences over demographic circumstances.

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responses might be biased so that demographic groups which are really at different standards of living actually report very similar standards of subjective well-being (Bradbury, 1989). More practically, these indicators are typically only weakly associated with income and family composition and thus require very large samples for accurate estimation.

Budget Standards Based

Budget standards involve researchers assembling a list of consumption goods needed to attain some given living standard, such as "modest but adequate" (e.g., Saunders *et al.*, 1998). These are then costed for different family types. Though this method produces precise estimates, it can be difficult to justify the assumptions needed to build the list of goods and the weights to be placed on each category of expenditure.

Consumption Theory Based

Several different approaches have been developed using data on household expenditure patterns, employing a variety of identifying assumptions. These include: that the food share is an indicator of household well-being (Engel, 1895); that family composition has only an income effect on some non-shared goods (Rothbarth, 1943); that composition has only a price effect (Barten, 1964); and that the equivalence scale is constant at all income levels (Lewbel, 1989; Blackorby and Donaldson, 1991).

Gorman summarized the price-like impact of household composition using the words of his schoolmaster: "When you have a wife and a baby, a penny bun costs threepence" (Gorman, 1976, p. 215). At the same time, when extra members enter the household there is only a small increase in the effective price of jointlyconsumed goods like heating, which are thus relatively cheaper per person. This equivalence between household size and price effects was first used by Barten (1964) to estimate price responses from data where all subjects faced the same prices. Subsequent research using this model has generally sought to do the opposite—use information on behavioral responses to price changes, together with information on consumption patterns in households of different sizes, to estimate the degree of joint consumption (e.g., Muellbauer, 1977; Nelson, 1988). This "Barten model" is used as the modeling framework in this paper, with an identification approach that is closer in spirit to Barten's original approach than that of the more recent research.

Even aside from any issues of empirical identification, however, the limitations associated with the simple structure of the Barten model are well recognized. In particular, the model does not account for differences in consumption preferences between household members and the within-household distribution of income. As Gorman (1976) also noted, threepence worth of penny buns fills three stomachs, but threepence worth of beer only satisfies the beer drinkers in the household. Nonetheless, it has been argued that this model might serve as a reasonable approximation for households of multiple adults (Nelson, 1988).

2. The Barten Equivalence Scale Model

The Barten consumption model can be considered as a special case of a more general model of household welfare and consumption technology. Consider a household consisting of two people. We assume that when either person *j* lives alone and has income *y*, they choose their consumption of market commodities q_{ij} so as to maximize a conventional utility function $u_j = U_j(q_{1j}, q_{2j}, \ldots, q_{lj})$ subject to their budget constraint $\sum_i p_i q_{ij} \leq y$.

When they share a household, household consumption is chosen so as to maximize a separable function of the welfare of each household member, subject to a household budget constraint. That is,

(1)
$$\max U(u_1, u_2)$$

subject to $\sum_i p_i Q_i(q_{i1}, q_{i2}) \le y$

The function $Q_i(q_{i1}, q_{i2})$ represents the household purchase requirement for commodity *i* (Lau, 1985). For goods that cannot be shared, it is simply the sum of the personal consumption amounts q_{ij} . However, for goods which have some degree of joint consumption or sharing, the purchase requirement will be less than this. The properties of this general household purchase function are discussed further in the Appendix.

The household welfare function U(.) can be interpreted in several ways. Most simply, it might be considered to represent the preferences of a "caring" but "non-paternalistic" household head who controls household consumption. The individual welfare functions might then be the head's views on the needs of the other household members. Becker (1981) shows that this interpretation can hold even when the other individuals have some control over their own consumption.

Alternately, if U(.) is additive, then the first order solution to this household decision problem is identical to the outcome of a Pareto efficient allocation of consumption between the household members (Panzar and Willig, 1976). The function U(.) can then be interpreted as a summary of the relative bargaining strengths of the individuals in the household. "Bargaining strength" in this context should be interpreted broadly, including the impact of altruistic feelings for the welfare of other household members. In general, U(.) might also be a function of other variables influencing bargaining within the household such as wage rates, private incomes, and social norms of within-household distribution. By definition, preferences over household composition itself do not enter U(.).

Including bargaining factors would make the present model similar to that in the "collective consumption" literature (Chiappori, 1988, 1992; Browning *et al.*, 1994; Apps and Rees, 1997). One difference is that most collective consumption models are unable to fully recover the household income-sharing rule because they do not assume that individuals' preferences are stable across household types (Browning *et al.*, 2006 is an exception). Here, as in all the equivalence-scale literature, this is a necessary identifying assumption.

To arrive at the Barten model, we introduce two additional simplifying assumptions: there is equal sharing of resources within the household, and the two individuals have the same preferences for commodities. That is, U(.) is assumed

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symmetric and $U_1(.)$ has the same functional form as $U_2(.)$. With these assumptions the purchase function for commodity *i* is simply $Q_i = r_i q_{i1} = r_i q_{i2}$ (see the Appendix). That is, $q_{i1} = q_{i2} \forall i$ and the household needs to purchase r_i times more of the commodity than each person consumes. If good *i* is not shared, $r_i = 2$ and the household has to purchase twice the consumption of each person, while if it is a pure public good within the household then $r_i = 1$ with each unit of purchase providing a unit of consumption for each person.

In these circumstances, the household faces a purchase decision problem of maximizing one of the individual welfare functions $U_j(q_{1j}, q_{2j}, \ldots, q_{Ij})$ (they are identical) subject to a household budget constraint $\sum_i p_i r_i q_{ij} \leq y$ (where j = 1 or 2). Since the symmetry assumptions imply equal sharing of income within the household, we can write the budget constraint in terms of the income received by each person as $\sum_i (p_i r_i/2) q_{ij} \leq y/2$, which makes it clear that the decision problem is the same as that for the one-person household, except that they are now allocating half the household income and are facing prices that are $r_i/2$ times market prices. The interpretation of the purchase function parameters r_i , and potential strategies for assigning reasonable bounds for them, are discussed further below. Once known, however, standard price index theory can be used to derive household equivalence scales.

Denoting the budget share of commodity group *i* by $w_i = q_i p_i / y$, a representative person living alone and with income y^0 consumes $q_i^0 = w_i^0 y^0 / p_i$ of each commodity and reaches welfare level u^0 . In the couple household, the Barten assumptions imply that the husband and wife consume the same amount of each commodity and income is equally shared between them. When the couple household purchases a quantity Q_i , of each commodity, each person consumes $q_{ij}^1 = Q_i / r_i$ and reaches a welfare level of u^1 . Personal consumption of each commodity can then be expressed in terms of household budget shares and income as $q_{ij}^1 = w_i^1 y^1 / r_i p_i$.

A Laspeyres equivalence scale (corresponding to a Laspeyres price index) for the cost of a couple relative to a single person can be defined as $m_L = \sum_i q_i^0 p_i r_i / \sum_i q_i^0 p_i$. The denominator is the expenditure required by a single person to consume the vector q^0 . The numerator is the expenditure required by the couple household so that each individual can consume the same vector q^0 . Using the relationships shown in the paragraph above, this simplifies to $m_L = \sum_i w_i^0 r_i$, the average relative purchase requirement for each commodity, weighted by the single-person budget shares.

Now q^0 is the bundle of goods chosen by the single-person household. It will not necessarily be the welfare-maximizing quantity for the people in the couple households and it is possible that couples could achieve the same welfare level at a lower total expenditure by substituting toward goods which are shared and are thus effectively cheaper. This means that the true equivalence scale at welfare level u^0 , must be less than m_L (or equal if there is no substitution).

Similarly, a Paasche equivalence scale can be calculated using coupleconsumption patterns as weights. This represents the cost of consuming the consumption bundle of the individuals when living as couples, and is defined

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as $m_P = \sum_i q_i^1 r_i p_i / \sum_i q_i^1 p_i = 1 / \sum_i w_i^1 \frac{1}{r_i}$, i.e. the harmonic mean of the relative purchase requirements, weighted by couple-income shares. Following similar rea-

soning to above, this scale will be a lower bound for the true equivalence scale calculated at welfare level $u^{1.5}$

In the main empirical analysis below, these scales are calculated at the mean budget shares of single and couple households. Plutocratic shares are used for the base results (total expenditure on good i divided by total expenditure). The geometric mean of the Laspeyres and Paasche scales is also calculated (the "Fisher ideal" scale).

When the Laspeyres and Paasche scales are calculated at the same welfare level, the bounds above can be combined to form upper and lower bounds for the true scale at that welfare level (and the Fisher scale is a reasonable compromise). However, unless singles and couples are on average equally well off (or preferences are homothetic) we would not expect their observed average budget shares to reflect the consumption patterns that would occur if they were at the same welfare level—and so combining the two scales is problematic.

To take account of this, we also present some scales where singles and couples are at approximately the same welfare level. This is calculated by starting from the budget share allocation of singles whose household income⁶ is in the middle quintile group of the income distribution of singles, calculating the Laspeyres scale, multiplying this by the average income of singles in the middle quintile to obtain the income required in the couple household to be at the same welfare level, then calculating the Paasche scale for couples at this income level (interpolated from quintile-specific scale calculations). As it turns out, there is not much variation in the Laspeyres and Paasche scales across income levels and so the Fisher scale calculated from this procedure is very close to the simple average of the Laspeyres and Paasche scales calculated at average budget shares (see Table 2 and Section 4.1 for more discussion).

2.1. Implications of the Barten Simplifications

More generally however, the Barten model does rest on a very restrictive model of household consumption allocations. Aged couples do not consist of identical twins, and we cannot assume that resources are shared equally between them. Are these simplifying assumptions likely to have much impact on the equivalence scales that are relevant to pension policy?

It is clear that the within-household sharing of income must be relevant to the true person-specific equivalence scale. If one member receives the bulk of

⁵It might also be noted that an alternative, apparently plausible, method for calculating an equivalence scale might be to calculate the arithmetic average of the commodity-specific scales with the couple budget shares as weights. Such a "naïve" scale leads to a higher estimate of the equivalence scale than either the Paasche or Laspeyres scales.

⁶These calculations are made by grouping by income rather than expenditure quintiles to avoid the endogeneity bias due to measurement error and transitory variations in expenditures. For example, expenditure on capital goods (such as white goods or car purchase which are averaged over a 12-month period) might lead to a household being in the top quintile of expenditure even though their consumption level is lower. Because capital goods tend to be public, this would distort the pattern of equivalence scales across groups.

household resources then they will need only a low two-person household income for them to have the same living standard they would have if single. The opposite applies to the other person. On average, these two effects cancel out; the extra income in the couple household for one person is equal to the reduced income for the other.

Even if unequal sharing of resources could be identified empirically, it is unlikely that this would be generally applied to pension policy. At face value, unequal within-household sharing suggests that categories of people who receive a greater share of resources in couple families should also receive a higher pension when single. This might be ethically justifiable if the within-household inequality arose from differences in socially-approved needs (e.g., one person has high medical expenses or nutritional needs), but would not be justifiable if it arose from inequality of power within the household. Given the difficulty in separating these determinants, it would seem reasonable to initially focus on an estimate of the average couple/single relativity.

As well, however, if the personal welfare function is concave, then an unequal distribution of resources within the household will mean a lower average welfare level than if the same resources were equally allocated (assuming identical cardinal welfare functions). Even if resources within retired couples are distributed equally on average (as evidence seems to suggest; see Bradbury, 1997), there is likely to be variation around this average. The results here do not take account of this withinhousehold inequality and hence will tend to underestimate the average relative needs of couple households. But this is only one example of the more general phenomena of income and need heterogeneity that are not addressed in poverty and inequality measurement. The results here are thus best interpreted as describing the relative needs of singles and couples that could be achieved if resources were equally shared within the couple.

The Barten model also assumes that each member of the household has the same consumption preferences. However, in practice these are likely to diverge significantly, particularly for narrowly defined commodity groups. In this situation the effective (or "shadow") price of the good in the two-person household can vary depending upon the consumption of the other member. In general, for goods that are partly public, a higher level of consumption by the second household member implies a lower shadow price for the first member (see Appendix). This effect is strongest for pure public goods where the household purchase requirements are simply the maximum of personal consumption levels. A person consuming less than the maximum can thus increase their consumption without the household needing to purchase more of the good—implying a shadow price of zero for this person but a market price for the maximum consumer. At the other extreme, the shadow price is always equal to the market price (and hence not sensitive to unequal consumption) for goods that are fully private. Conveniently, these are also the goods where unequal consumption is most prevalent, for example, men's and women's clothing.

Nonetheless, for goods which are public or semi-public within the household, prices will vary according to the consumption of each member. On average, these variations will tend to offset each other. Holding constant the overall between-person distribution of resources, if a person is the primary consumer of commodity

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A, they will be less likely to be the primary consumer of commodity B. These offsetting effects mean that the impact on the average equivalence scale that they face will be small (though non-linearities mean that there may be some differences). This is confirmed in Bradbury (1997) where a model of the more general form described in the Appendix is estimated, and equivalence scales are derived that are very close to those derived when using the Barten assumptions.

2.2. Implications of Home Production

Bradbury (1997) also tests whether the actual consumption patterns of households are consistent with this consumption framework. The main divergence is found in prepared food consumption; couples spend more on food than the consumption patterns of singles and the sharing assumptions would suggest. These changes probably arise from the incentives associated with home production. Because the time required to cook for two is not much more than the time required to cook for one, there are strong incentives for couples to engage in more home food preparation.

It is not clear, however, that pension policy should take these time costs into account. These patterns of consumption imply that pensioners do value their time—they spend less time on activities that yield less output. Nonetheless, they still have much of what, by average community standards, might be considered "free" time. Current discourse on public pension policy does not include discussion of compensation to single pensioners for their lost efficiency of home production time. These results in this paper follow this convention of not considering these time costs.⁷ Again, this points to the necessarily central role of normative assumptions in the estimation of policy-relevant consumer equivalence scales.

3. Estimates of the Relative Needs of Older Single Person and Couple Households

The estimation of relative needs in this model requires information on the expenditure shares of singles and couples on different commodity groups, and the magnitudes of the relative purchase requirement parameters, r_i . The budget shares of total current expenditure are estimated from the Australian Bureau of Statistics Household Expenditure Surveys of 1988–89, 1993–94, 1998–99, and 2003–04. Attention is confined to households with one adult or with two adults of opposite sex, all of whom are Age Pension age or older (65 for men, 62 for women in 2003–04, 60 for women in other years). To control for wealth effects attention is restricted to home-owning households (with or without a mortgage). This includes four-fifths of retired households. Costs for renters are examined separately in Section 4.

Rather than attempting to estimate the relative purchase requirements, r, using their affinity with price effects, they are treated here as assumed

⁷See Bittman (1991) for a discussion of the gender differences in home production in older households and Bradbury (2008) for a model of the costs of children incorporating home production. If economies of home production time were included as relative benefit for couples, this would reinforce the conclusion of this paper that couples are better off under the existing pension relativities.

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technological features of household consumption, albeit influenced by social norms of consumption. Some goods are close enough to entirely private (e.g., men's and women's clothing) to make an assumption of pure private (r = 2) reasonable. Most goods, however, have some features that imply that the household will need to purchase less than twice the amount that is consumed by each person. Can we conceptualize the technology of consumption in a way that helps us formulate reasonable assumptions about this degree of sharing?

One approach is to conceptualize these semi-public goods as part pure-private and part pure-public (the quasi-linear model in the Appendix). Let t_i denote the proportion of good *i* that is allocated to private consumption in the two-person household (of which half is consumed by each person) and $1 - t_i$ the proportion consumed as a pure public good (of which each person consumes the full amount). Then, each person will consume $q_{ij} = t_i q_i/2 + (1 - t_i)q_i$ which implies that $q_i = 2/(2 - t_i)q_{ij}$ and hence that $r_i = 2/(2 - t_i)$. In the Appendix, more general formulations for semi-public goods are described which permit unequal consumption (following Lau, 1985). However, this simple equal consumption framework is more useful for the introduction of modeling assumptions.

As an example, consider the running costs of a car on a given day. If the car travels 1 km taking (only) person 1 to a destination, 1 km for person 2, and 1 km to a destination for both people, then t = 2/3 and r = 1.5. That is, each person travels 2 km, but the car must travel 3 km. The running costs for the household of two people are thus 1.5 times the running costs associated with the consumption of a single person.

Goods that are essentially private but which involve a fixed wastage overhead can be conceptualized in the same way. If on, average, each individual consumes 950 ml of milk per day and the last 100 ml of household milk consumption is wasted, we can think of this 5 percent wastage out of the 2 liter consumption in the two-person household as the public fraction, implying that the relative purchase requirement of the two-person household is 2/(2 - 0.95) = 2000/1050 = 1.905.

This example also illustrates one limitation of the modeling framework—it does not consider economies of scale of the production function type. That is, the same wastage efficiencies gained from the two-person household should also be available to a single-person household whose occupant drinks twice as much milk. The model could in principle be generalized to include such characteristics of production, but here we focus only on variation across household composition and the modeling assumptions made below should thus be considered as applying to average consumption levels.

Introducing assumptions about consumption sharing is easier the more detailed the commodity specification, but this makes the methodology less transparent. A compromise approach is to group commodities according to their relative purchase requirements, as is done in Table 1. The table shows two representations of the relative purchase requirements of couple households. The first set of data columns shows the author's assumptions of the amount needed to be purchased by the couple household in order for each individual to have one unit of personal consumption (the r_i parameters). Low, preferred, and high values for these parameters are given. Values of 1 indicate pure public goods, 2, pure private. The relative shadow price facing the individuals in the couple household is half the r_i value. The second set expresses these same relationships from the perspective of

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TABLE 1

COMMODITY CATEGORIES AND RELATIVE PURCHASE REQUIREMENT ASSUMPTIONS

			Assu	med Degree of	Sharing		
Expenditure Categories		Relativ (r: 1 = Pure	e Purchase R Public, 2 = P	equired ure Private)	Fraction Private	of Good $(t = 2(1 - 1))$	That Is - 1/r))
Title	Description	Low	Pref.	High	Low	Pref.	High
Housing Fuel Prepared food	Repairs and maintenance, rent, land and water supply taxes Electricity, gas etc (not transport fuels) Foods that require preparation and/or are perishable such as flour, rice, pasta,	1.00 1.20 1.60	1.15 1.30 1.75	$1.30 \\ 1.40 \\ 1.90$	$\begin{array}{c} 0.00 \\ 0.33 \\ 0.75 \end{array}$	0.26 0.46 0.86	$\begin{array}{c} 0.46 \\ 0.57 \\ 0.95 \end{array}$
Eat out Personal food	vegetables, bread, unprocessed meat and milk Restaurants, take-away food Biscuits, fruit, processed meat, breakfast cereals, cakes, non-alcoholic drinks, dairy	$1.90 \\ 1.80$	1.95 1.90	2.00 2.00	$0.95 \\ 0.89$	0.97 0.95	$1.00 \\ 1.00$
Alcohol Tobacco Clothing Shared furnishings &	products (other than mulk), spreads, tea, conce, contectionary, tinned fish, etc. Alcohol Tobacco Clothing Lounge room, kitchen and garden furniture, art, major appliances and household tools	1.80 2.00 1.10	1.90 2.00 1.20	2.00 2.00 1.40	$\begin{array}{c} 0.89\\ 1.00\\ 1.00\\ 0.18\end{array}$	$\begin{array}{c} 0.95\\ 1.00\\ 1.00\\ 0.33\end{array}$	$\begin{array}{c} 1.00\\ 1.00\\ 1.00\\ 0.57\end{array}$
equipment Other furnishings Household shared	Floor coverings, curtains, other furniture Gardening services, nails, screws etc.	$1.20 \\ 1.00$	$1.30 \\ 1.05$	$1.40 \\ 1.10$	$0.33 \\ 0.00$	$0.46 \\ 0.10$	$0.57\\0.18$
Operation Communication Cleaning Health insurance Medical Transport fares Vehicle fixed costs Vehicle running Shared recreation	Telephone and post Soaps and detergents (not personal), wraps, gardening products etc Health insurance Dental and medical fees and medications Air, bus, rail fares etc (excluding holiday fares) Vehicle registration and insurance, purchase, accessories etc Vehicle operating costs such as petrol, vehicle servicing etc Shared goods such as newspapers, televisions, stereos and associated supplies; pets,	1.20 1.80 2.00 2.00 1.00 1.20	1.30 1.95 1.95 1.95 1.30 1.30 1.20	1.50 1.50 2.00 2.00 1.10 1.40	$\begin{array}{c} 0.33\\ 0.33\\ 0.89\\ 1.00\\ 0.95\\ 0.00\\ 0.00\\ 0.33\\ 0.00\end{array}$	$\begin{array}{c} 0.46\\ 0.46\\ 0.95\\ 1.00\\ 0.97\\ 0.10\\ 0.10\\ 0.33\\ 0.33\end{array}$	$\begin{array}{c} 0.67\\ 0.67\\ 1.00\\ 1.00\\ 1.00\\ 0.18\\ 0.57\\ 0.57\\ 0.57\end{array}$
Personal recreation Personal care Gifts and shared misc Misc not shared	general holiday expenditures Books, magazines, gambling, sports, admission charges, and holiday travel. Hairouts, tolierise and cosmetics etc Gifts, misc property payments, personal advertising, etc Child support/alimony payments, pevellery, and accessories, education fees,	1.60 1.80 1.00 1.80	1.75 1.90 1.10 1.90	1.90 2.00 2.00 2.00	0.75 0.89 0.00 0.89	$\begin{array}{c} 0.86 \\ 0.95 \\ 0.18 \\ 0.95 \end{array}$	$\begin{array}{c} 0.95 \\ 1.00 \\ 0.33 \\ 1.00 \end{array}$
Misc part shared	protessional association subscriptions, etc Miscellaneous commodities and services nec, stationary, fees and fines, non-housing interest payments, etc	1.20	1.50	1.80	0.33	0.67	0.89

the quasi-linear model of purchase requirements, where the good is assumed to comprise two parts, one pure private and one pure public. The t_i parameters show the fraction of the good that is private.

A few goods (clothing, tobacco, health insurance, transport fares) are assumed to be purely private. Most other goods are assumed to be either close to private or close to public (see also Figure 1). Goods that are assumed close to private include alcohol and personal food such as biscuits, fruit, processed meat, breakfast cereals, cakes, non-alcoholic drinks, dairy products (other than milk), spreads, tea, coffee, confectionary, and tinned fish. Even though each unit of food is only consumed by one person, these are assumed not to be fully private because wastage means that singles need to purchase more than half the amount of couples in order to have the same consumption. For these goods, the low, preferred, and high relative requirements assumptions are set at 1.8, 1.9, and 2.0, respectively. Equivalently, we can think of these goods as having between zero and 11 percent of a public component– which in this case can be interpreted as the fraction that is wastage in the couple household.

In general, it might be possible to gather this data in other ways, for example via in-depth studies of food wastage, studies of which types of journeys are undertaken singly or in company, or consultations with people in older households similar to the focus group consultations undertaken in budget standards studies. To take another example, household expenditure on fuel predominantly comprises water heating, home heating/cooling, and cooking. The first of these is primarily used for bathing and has little joint consumption (unless people bathe together), while joint consumption is substantial for the others. Data collected by the utility industries on the relative importance of these different components in typical households could be used to provide more precise scale economy bounds than given here.

Returning to Table 1, other close-to-private goods include eating out (a negligible amount of meal sharing is assumed), prepared food (a larger wastage fraction than personal food), personal hygiene goods (mainly toilet paper and tissues, assumed not shared), medical fees (less per-person wastage of non-prescribed medications in couple households), personal care (some sharing of toiletries), and miscellaneous goods that are likely to be personally consumed.

On the other hand, housing is assumed to be close to fully public, with couples requiring not much more housing than singles. This assumption is based on social norms of housing consumption in Australia, which in turn derive from the limited liquidity of owner-occupied housing. It is assumed that housing is not perfectly public because it might be considered normal for members of a couple to have slightly more space to accommodate activities only undertaken by one member (e.g., a sewing room). The preferred estimate assumes that about one-quarter of the value of a house is privately consumed and the remainder public (though the suggested bounds range from an assumption of fully public to 46 percent public).

Other goods which are closely linked to housing are assumed to have a similar degree of sharing (fuel, furniture, household operation, cleaning, shared recreation goods). Telephone and postal costs are assumed to be substantially shared because of overlaps between the social contacts of the couple. Vehicle costs are split into

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fixed costs (it is assumed that a couple will not need an extra vehicle) and running costs, where it is assumed that vehicles owned by couples need to go on 20–40 percent more journeys to attain the same mobility as obtained by a single person.

The observed average budget shares in 2003–04 for singles and married couples over Age Pension age are shown in Table 2. Goods that have budget shares over 5 percent are shown in bold to aid identification of the most important goods in the equivalence scale calculation. These are housing (mainly maintenance and taxes), food, medical expenses, vehicle costs, and recreation. Couples tend to spend a lower proportion of their total expenditure on goods such as housing which have a high degree of joint consumption. Some of the differences between singles and couples might also reflect the fact that singles are generally older. Variations across age are considered in Section 4.

At the preferred values of the relative purchase requirements for couples, the Laspeyres scale (based on the singles budget share) yields a value of 1.48, and the Paasche scale, based on the expenditure patterns of couples, a scale of 1.44. A much greater variation arises if we base conclusions on the low or the high assumptions for the commodity-specific scales. The Fisher scale (the average of Laspeyres and Paasche) ranges from 1.35 to 1.58, with a preferred value of 1.46. The pre-2009 relativity in the Australian Age Pension, of 1.64, is greater than all these estimates, implying that home-owning couples reliant solely on the Age Pension had a higher living standard than corresponding single people.

The bottom panel of the table also shows the Fisher scale calculated from the budget shares of singles in the middle income quintile group (of singles) and of corresponding middle-income couples. These scales are marginally higher than the scales calculated from the overall budget shares shown in the table (1.47 vs. 1.46 for the preferred scale). The last line of the table also shows the impact of using the iterative approach described in Section 3 which ensures that the budget shares represent the consumption patterns of couples and singles at approximately the same welfare level. These are marginally higher again (1.48). Because these differences are so small, and because of the greater statistical precision of the overall budget shares are used as the base estimates here.

The final column of Table 2 shows a set of r values chosen to ensure that the Fisher scale (based on the overall budget shares) will be equal to the pre-2009 pension relativity.⁸ Though this is not a unique scaling, this suggests that high relative purchase requirements for couples might be needed in order to justify the current pension relativity. For example, couples might be required to spend 1.38 times that of singles to attain the same per-person standard of housing consumption.

Undertaking the budget share calculation for the years 1988–89, 1993–94, 1998–99, and 2003–04 yields estimates for the Fisher preferred scale of 1.49, 1.48, 1.47, and 1.46 for the four years. This steady fall in relative needs has been driven by falls in the budget shares of home-eaten food and clothing, together with

⁸As noted above, $r_i = 2/(2 - t_i)$ and so $t_i = 2(1 - 1/r_i)$, which is bounded between 0 and 1. Let $L_i = \ln(t_i/(1 - t_i))$, $L_i^* = a + L_i$, $t_i^* = 1/(1 + \exp(-L_i^*))$, $r_i^* = 2/(2 - t_i^*)$ and calculate the Fisher equivalence scale based upon r_i^* . Then adjust *a* until the Fisher scale equals the current pension relativity of 1.64.

Expenditure Category	Budget Share (>5% in Bold)		Relative Needs for Couples (r)			Implied
	Singles	Couples	Low	Preferred	High	Current
Housing	0.182	0.089	1.00	1.15	1.30	1.38
Fuel	0.042	0.034	1.20	1.30	1.40	1.60
Prepared food	0.065	0.077	1.60	1.75	1.90	1.91
Eat out	0.039	0.040	1.90	1.95	2.00	1.99
Personal food	0.078	0.091	1.80	1.90	2.00	1.97
Alcohol	0.018	0.025	1.80	1.90	2.00	1.97
Tobacco	0.004	0.006	2.00	2.00	2.00	2.00
Clothing	0.027	0.031	2.00	2.00	2.00	2.00
Shared furnishings & equipment	0.041	0.035	1.10	1.20	1.40	1.46
Other furnishings	0.014	0.025	1.20	1.30	1.40	1.60
Household shared operation	0.028	0.018	1.00	1.05	1.10	1.15
Communication	0.037	0.029	1.20	1.30	1.50	1.60
Cleaning	0.012	0.013	1.20	1.30	1.50	1.60
Hygiene	0.003	0.004	1.80	1.90	2.00	1.97
Health insurance	0.026	0.034	2.00	2.00	2.00	2.00
Medical	0.069	0.048	1.90	1.95	2.00	1.99
Transport fares	0.006	0.002	2.00	2.00	2.00	2.00
Vehicle fixed costs	0.060	0.089	1.00	1.05	1.10	1.15
Vehicle running expenses	0.050	0.060	1.20	1.30	1.40	1.60
Shared recreation	0.050	0.066	1.00	1.20	1.40	1.46
Personal recreation	0.059	0.094	1.60	1.75	1.90	1.91
Personal care	0.021	0.022	1.80	1.90	2.00	1.97
Gifts and shared misc	0.038	0.032	1.00	1.10	1.20	1.28
Misc not shared	0.005	0.006	1.80	1.90	2.00	1.97
Misc part shared	0.025	0.030	1.20	1.50	1.80	1.78
Sample size	472	533				
Upper bound equivalence scale (Laspeyres)			1.38	1.48	1.60	1.65
Lower bound equivalence scale (Paasche)			1.32	1.44	1.57	1.63
Geometric mean (Fisher ideal)			1.35	1.46	1.58	1.64
(Jackknife standard error)			(0.011)	(0.010)	(0.010)	
Inverse (singles/couples)						
Upper bound equivalence scale (Laspeyres)			0.727	0.674	0.624	0.605
Lower bound equivalence scale (Paasche)			0.757	0.694	0.639	0.614
Geometric mean (Fisher ideal)			0.742	0.683	0.631	0.610
Coomatria maan (Eicher idec)			1.25	1 47	1 50	
Geometric mean at approx same			1.35	1.47	1.37	
welfare level			1.30	1.40	1.00	

TABLE 2 2003–04 Budget Shares and Equivalence Scales Based on Alternative Relative Need Assumptions

Note: Bold type indicates goods that have budget shares over 5 percent.

Source: ABS Household Expenditure Survey 2003–04, Confidentialized unit record file. Author's relative needs assumptions.

increases in the budget shares of vehicle fixed costs and housing. These trends have been partly offset by increases in eating out, medical expenses, and personal recreation. Figure 1 plots these changes in budget shares against the degree of sharing for each commodity. There are few goods in the bottom-left of the figure,



Figure 1. Trend Change in Budget Share 1988–89 to 2003–04 by Assumed Relative Needs of Couples

Note: Trend change in budget share is estimated as a linear trend through the budget shares for each of the four years (average of couple and single trend).

implying a general increase in the budget share among goods that have greater economies of sharing.

The reasons for these changes in expenditure patterns probably include income effects (e.g. the elderly are now richer and more likely to purchase vehicles), price effects (e.g. clothing is cheaper), and possibly also taste changes. But whatever the reasons, the trend is clearly towards increases in the relative needs of singles. Alternative assumptions about the degree of commodity sharing are not likely to change this conclusion, unless they are so large as to move more goods into the bottom-left corner of Figure 1.⁹

⁹See Blundell and Lewbel (1991) and Banks and Johnson (1994) for more discussion of the implications of price changes for changes in consumer equivalence scales.

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4. EXTENSIONS

4.1. Cost Variations with Age and Income

The single elderly are on average older than those living in couples. Does this affect the calculations of the relative needs of singles and couples? The above calculations were repeated for young and old households. Young households are single or couple households where the male (if present) is aged 65–69 and the female (if present) is aged 62–69. In old households the members are aged 75 or higher. Old households tend to spend a larger fraction of their total expenditure on housing and medical care, and a smaller fraction on vehicle fixed costs (e.g., purchases), personal recreation (e.g., travel), and eating out.¹⁰ However, there is no clear tendency for older households to shift their consumption toward goods that are either relatively public or private. The result is that the estimates of relative needs are very similar. For both the young and old groups, the preferred relative need Fisher scale is 1.47, only slightly higher than the overall estimate above of 1.46.

Similarly, the estimates in the previous section are for single and couple Australians of Age Pension age. Restricting the analysis to those actually receiving income support payments (the poorer three-quarters of the population), the estimates are also slightly larger, with the Fisher relativities ranging from 1.36 to 1.59, with a preferred value of 1.47.

A more detailed investigation of budget allocation across income¹¹ quintile groups does yield some apparent differences. Singles and couples are separately classified into quintile groups based on disposable income (e.g., the 20 percent of singles with the lowest income assigned to quintile group 1). The simple Fisher relativities based on the preferred scales are 1.44, 1.48, 1.47, 1.49, and 1.46 for the low to high income groups, respectively. Alternatively, starting from the single quintile groups and using the interpolation procedure described in Section 2 to estimate the scales when couples are at approximately the same welfare level, yields estimates of 1.44, ¹² 1.45, 1.48, 1.48, and 1.46. These results suggest that couples at the top and bottom of the income distribution might need less than those in the middle of the distribution—but the differences are not large.

4.2. Equivalence Scales for Private Renters

All the above calculations are based on the consumption patterns of home owners. Though this is by far the most common housing situation of the elderly in Australia, there are still substantial numbers of elderly who do not own their own homes. The 2003–04 HES, for example, reports that, of those people of Age Pension age living in private households, 86 percent owned their own home (some with mortgages), 5 percent were paying rent to a government landlord, 7 percent to other landlords, and 2 percent were living in other tenure arrangements (including rent-free).

¹⁰Tables showing these budget shares are available in Bradbury (2009).

¹¹See footnote 6.

¹²Interpolation is not possible for the bottom quintile, and it is necessary to assume that the Paasche scale is constant within the whole of the bottom quintile of couples.

The Age Pension recognizes the additional costs of renters by providing Rent Assistance to pension recipients renting in the private market. Singles are actually paid slightly more than couples in recognition of the strong economies of sharing associated with accommodation costs. For single and couple renters receiving the maximum rate of payment, the payment ratio for all payments combined was 1.53 prior to September 2009 (compared to 1.64 for non-renters).¹³

For home owners, housing costs make up 9 and 18 percent of the budget for couples and singles, respectively, whereas for renters (from a non-government landlord), housing costs amount to 27 and 38 percent on average. Since housing is very much shared, we would expect this difference in expenditure patterns to be associated with a lower estimate of couple relative needs, and this is indeed the case. For renters, the preferred Fisher scale is 1.40 (compared to 1.46 for owners). Using the high relative needs assumptions the Fisher scale is 1.53, which is equal to the actual pre-2009 pension relativity.

4.3. Unrelated Two-Person Households

What impact does sharing with a person other than one's spouse/partner have on relative expenditure needs? Among non-partnered people over Age Pension age, about 22 percent live with other people—13 percent with just one other person and 9 percent with two or more (2003-04 HES). These multi-person households can take advantage of some aspects of household joint consumption, but not others typically available to couples (e.g., they are unlikely to share a bedroom). The model used here can be also used to consider the situation of two unrelated people sharing a household—even if there are insufficient people in the survey data to reliably calculate their budget shares. This is done by using the Laspeyres scale, which only requires information on the budget shares of single-person households. This data, when combined with a revised set of sharing assumptions, can then be used to obtain relative need estimates. This is done in Bradbury (2009), where it is concluded that unrelated pairs would require 1.62 times the expenditure of singles (compared to 1.48 for the Laspeyres scale for couples). Of course, this estimate, like all those here, takes no account of the direct benefits of household composition-the autonomy of solitude or the joys of company.

5. CONCLUSION

Based on the modeling framework and assumptions outlined above, it is concluded that Australian single and couple home-owners reliant on Age Pension will have the same effective commodity consumption levels when the pension for couples is between 1.32 and 1.60 times the single pension (with a preferred value of 1.46). All these values are lower than the pre-2009 pension relativity of 1.64.

In 2009 a review of the Australian Age Pension system recommended increases to the single rate of Age Pension (Harmer, 2009). The research reported

¹³For singles, the base rate of payment in August 2009 was \$599 per fortnight (including utility, pharmaceutical, and telephone allowances). They were also entitled to a maximum of \$112 per fortnight in rent assistance if they were paying more than \$248 per fortnight in rent (reduced by 75c in the dollar for lesser rental amounts). The corresponding amounts for couples were \$981, \$105, and \$303.

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here was one source of evidence drawn upon by the review. Subsequently, increases in the pension were announced, taking effect in September 2009, bringing the relativity between singles and couples down to around 1.5-within the "plausible bounds" considered here. These bounds are based on a set of assumptions about upper and lower bounds for joint consumption together with household survey data on average budget shares.

The methodology here can also be used in applications where there is very limited survey data. Among private renters (a small fraction of the Australian aged population), the required relativities are lower because housing comprises a larger share of the household budget. For this group the couple relativity ranges from 1.26 to 1.54 times the single rate, with a preferred value of 1.40.¹⁴ Similarly, the relativity for two-person households who are not couples (e.g., siblings living together), can be estimated based on the consumption patterns of single adults combined with different sharing assumptions. All these estimates relate to the allocation and sharing of purchased commodities within the household. No account is made of preferences for different household types, home production, or the possible behavioral effects of income support policies.

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¹⁴The pre-2009 relativity of 1.53 for maximum rent assistance recipients falls at the edge of this range.

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SUPPORTING INFORMATION

Additional Supporting Information may be found in the online version of this article at the publisher's web-site:

Appendix: Extensions

Figure 2: Household consumption possibility frontiers for a single commodity in a 2-person household